# Confidence Intervals for AP Statistics

### Proportions

Name	Statistic	Parameter	Conditions	Formula	Calculator
One-sample z- interval for a proportion	ŷ	р	<ul> <li>Random sample</li> <li>n ≤ 10%N</li> <li>np̂ ≥ 10 and n(1 − p̂) ≥ 10</li> </ul>	$\hat{p} \pm z^* \sqrt{\frac{\hat{p}(1-\hat{p})}{n}}$	1-PropZInt
Two-sample z- interval for a difference in proportions	$\hat{p}_1 - \hat{p}_2$	$p_1 - p_2$	<ul> <li>Independent random samples or randomized experiment</li> <li>n₁ ≤ 10%N₁ and n₂ ≤ 10%N₂</li> <li>n₁p̂₁ ≥ 10, n₁(1 - p̂₁) ≥ 10 n₂p̂₂ ≥ 10, n₂(1 - p̂₂) ≥ 10</li> </ul>	$(\hat{p}_1 - \hat{p}_2) \pm z^* \sqrt{\frac{\hat{p}_1(1 - \hat{p}_1)}{n_1} + \frac{\hat{p}_2(1 - \hat{p}_2)}{n_2}}$	2-PropZInt

#### Means

Name	Statistic	Parameter	Conditions	Formula	Calculator
One-sample <i>t</i> - interval for a mean or paired t-interval	$ar{x}$	μ	<ul> <li>Random sample or randomized experiment</li> <li>n ≤ 10%N</li> <li>Population distribution is ≈ normal (given or sample data show no strong skew or outliers) or n ≥ 30</li> </ul>	$\bar{x} \pm t^* \frac{s}{\sqrt{n}}$ df = n - 1	TInterval
Two-sample <i>t</i> - interval for a difference in means	$\bar{x}_1 - \bar{x}_2$	$\mu_1 - \mu_2$	<ul> <li>Independent random samples or randomized experiment</li> <li>n<sub>1</sub> ≤ 10%N<sub>1</sub> and n<sub>2</sub> ≤ 10%N<sub>2</sub></li> <li>For each sample or group, the population distribution is ≈ normal (given or sample data show no strong skew or outliers) or n ≥ 30</li> </ul>	$(\bar{x}_1 - \bar{x}_2) \pm t^* \sqrt{\frac{(s_1)^2}{n_1} + \frac{(s_2)^2}{n_2}}$ df = smaller of n <sub>1</sub> – 1 and n <sub>2</sub> – 1 OR df = use technology	2-SampTInt

## Slope

Name	Statistic	Parameter	Conditions	Formula	Calculator
t-interval for a slope	b	β	<ul> <li>Relationship between x and y is fairly linear</li> <li>n ≤ 10%N</li> <li>For each x, the distribution of y is ≈ normal</li> <li>For each x, y has the same standard deviation</li> <li>Random sample or randomized experiment</li> </ul>	$b \pm t^* SE_b$ df = n – 2	LinRegTInt



# Significance Tests for AP Statistics

### Proportions

Name	Null Hypothesis	Conditions	Formula	Calculator
One-sample z- test for a proportion	H <sub>0</sub> : p = p <sub>0</sub>	• Random sample • $n \le 10\%$ N • $np_0 \ge 10$ and $n(1 - p_0) \ge 10$	$z = \frac{\hat{p} - p_0}{\sqrt{\frac{p_0(1 - p_0)}{n}}}$	1-PropZTest
Two-sample <i>z</i> - test for a difference in proportions	$H_0: p_1 - p_2 = 0$	<ul> <li>Independent random samples or randomized experiment</li> <li>n₁ ≤ 10%N₁ and n₂ ≤ 10%N₂</li> <li>n₁p̂<sub>c</sub> ≥ 10, n₁(1 − p̂<sub>c</sub>) ≥ 10 p̂<sub>c</sub> = X₁+X₂/n₁+n₂</li> <li>n₂p̂<sub>c</sub> ≥ 10, n₂(1 − p̂<sub>c</sub>) ≥ 10</li> </ul>	$z = \frac{(\hat{p}_1 - \hat{p}_2) - 0}{\sqrt{\frac{\hat{p}_c(1 - \hat{p}_c)}{n_1} + \frac{\hat{p}_c(1 - \hat{p}_c)}{n_2}}}$	2-PropZTest

### Means

Name	Null Hypothesis	Conditions	Formula	Calculator
One-sample <i>t</i> - test for a mean or paired <i>t</i> -test	$H_0: \mu = \mu_0$	<ul> <li>Random sample or randomized experiment</li> <li>n ≤ 10%N</li> <li>Population distribution is ≈ normal (given or sample data show no strong skew or outliers) or n ≥ 30</li> </ul>	$t = \frac{\bar{x} - \mu_0}{\frac{s}{\sqrt{n}}}$ df = n - 1	T-Test
Two-sample <i>t</i> - test for a difference in means	$H_0: \mu_1 - \mu_2 = 0$	<ul> <li>Independent random samples or randomized experiment</li> <li>n<sub>1</sub> ≤ 10%N<sub>1</sub> and n<sub>2</sub> ≤ 10%N<sub>2</sub></li> <li>For each sample or group, the population distribution is ≈ normal (given or sample data show no strong skew or outliers) or n ≥ 30</li> </ul>	$t = \frac{(\bar{x}_1 - \bar{x}_2) - (\mu_1 - \mu_2)}{\sqrt{\frac{(s_1)^2}{n_1} + \frac{(s_2)^2}{n_2}}}$ df = smaller of n <sub>1</sub> - 1 and n <sub>2</sub> - 1 OR df = use technology	2-SampTTest

### Slope

Name	Null Hypothesis	Conditions	Formula	Calculator
t-test for a slope	$H_0: \beta = \beta_0$	<ul> <li>Relationship between x and y is fairly linear</li> <li>n ≤ 10%N</li> <li>For each x, the distribution of y is ≈ normal</li> </ul>	$t = \frac{b - \beta_0}{SE_b}$	LinRegTTest
		<ul><li>For each x, y has the same standard deviation</li><li>Random sample or randomized experiment</li></ul>	df = n – 2	



# Chi-Square

Name	Hypotheses	Conditions	Formula	Calculator
$\chi^2$ test for goodness-of-fit	H <sub>0</sub> : The claimed distribution of (categorical variable) is correct. H <sub>a</sub> : The claimed distribution of (categorical variable) is incorrect.	<ul> <li>Random sample or randomized experiment</li> <li>n ≤ 10%N</li> <li>All expected counts &gt; 5</li> </ul>	$\chi^{2} = \sum \frac{(observed - expected)^{2}}{expected}$ df = # of categories - 1	χ²GOF-Test
$\chi^2$ test for homogeneity	H <sub>0</sub> : There is no difference in the distribution of (categorical variable) across populations or treatments. H <sub>a</sub> : There is a difference in the distribution of (categorical variable) across populations or treatments.	<ul> <li>Random samples from each population or randomized experiment</li> <li>n ≤ 10%N</li> <li>All expected counts &gt; 5</li> </ul>	$\chi^{2} = \sum \frac{(observed - expected)^{2}}{expected}$ df = (# of rows - 1) (# of columns - 1)	$\chi^2$ -Test
$\chi^2$ test for independence	H <sub>0</sub> : There is no association between two categorical variables in a given population or the two categorical variables are independent. H <sub>a</sub> : Two categorical variables in a population are associated or dependent.	<ul> <li>Random sample or randomized experiment</li> <li>n ≤ 10%N</li> <li>All expected counts &gt; 5</li> </ul>	$\chi^{2} = \sum \frac{(observed - expected)^{2}}{expected}$ df = (# of rows - 1) (# of columns - 1)	$\chi^2$ -Test

